

ES. N294, PAG 165

? $a \in \mathbb{R}$ $f(x) = \frac{x^2 + ax + 2}{x-4}$ non esiste
 ne max ne min relativi.

Domínio: $D_f = \{x \in \mathbb{R} \mid x-4 \neq 0\} = (-\infty, 4) \cup (4, +\infty)$

$$f'(x) = \frac{(2x+a)(x-4) - x^2 - ax - 2}{(x-4)^2} =$$

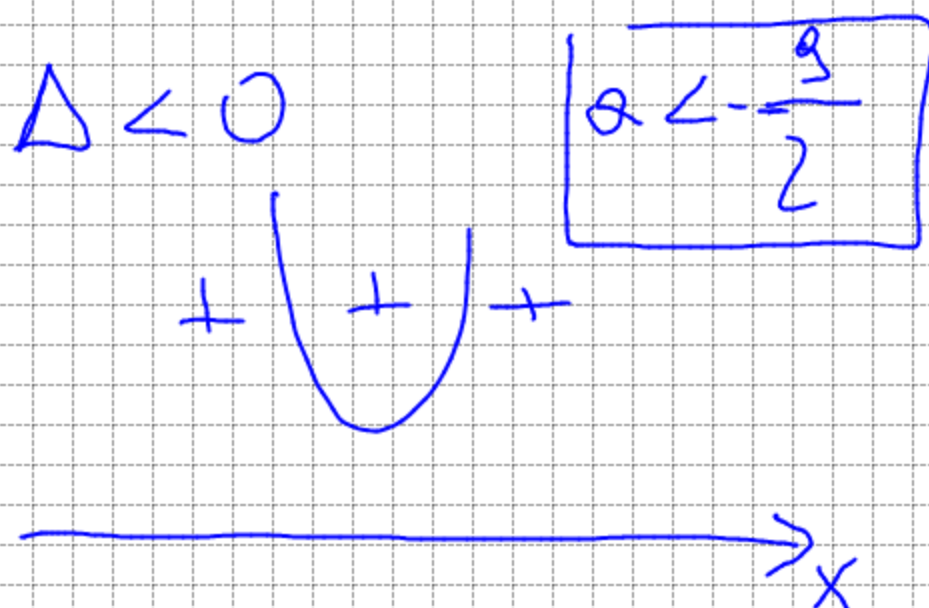
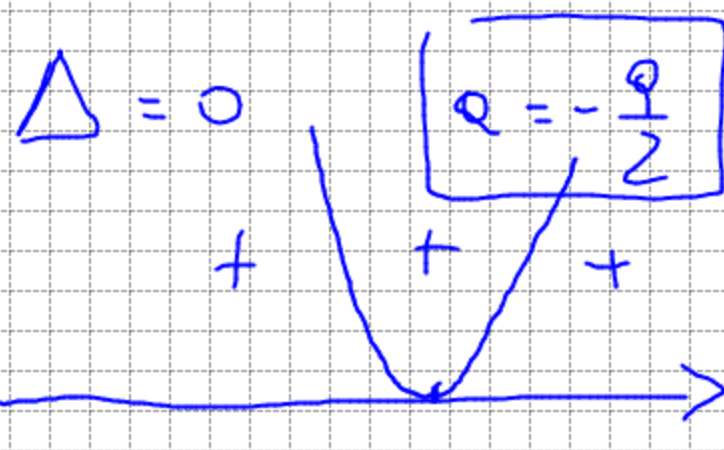
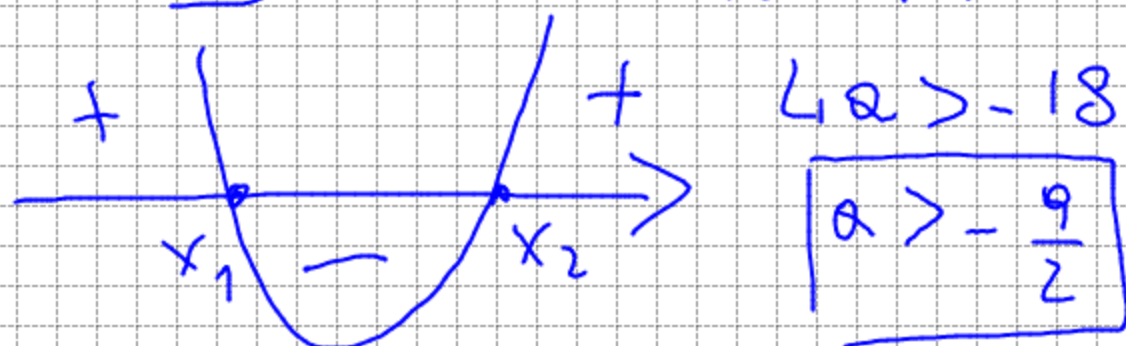
$$= \frac{2x^2 - 8x + ax - 4a - x^2 - ax - 2}{(x-4)^2} =$$

$$= \frac{x^2 - 8x - 4a - 2}{(x-4)^2} \geq 0$$

N) $x^2 - 8x - 4a - 2 \geq 0$

D) sempre +, $x \neq 4$

N) $\Delta > 0$ $16 + 4a + 2 > 0$



Se $a = -\frac{9}{2}$ $f'(x) = \frac{x^2 - 8x + 16}{(x-4)^2} =$
 $= \frac{(x-4)^2}{(x-4)^2} = 1$

Se $a \leq -\frac{9}{2}$ non si hanno ne max ne min relativi.

$f(x) = x e^{\sqrt{x+3}}$ max e min.

$D_f = \{x \in \mathbb{R} / x+3 \geq 0\} = [-3, +\infty)$

Segno:

$f(x)$ è positiva per $x > 0$

$f(x) = 0$ per $x = 0$

$f(x) < 0$ per $x < 0$

• max e min:

$f'(x) = e^{\sqrt{x+3}} + x e^{\sqrt{x+3}} \left(\frac{1}{2\sqrt{x+3}} \right) =$

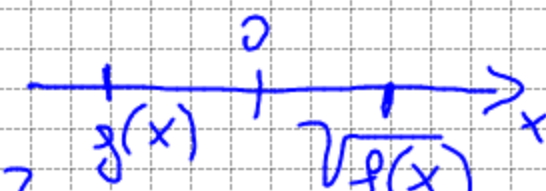
$P_1: e^{\sqrt{x+3}} \geq 0$ sempre + $\left(1 + \frac{x}{2\sqrt{x+3}} \right) \geq 0$

$P_2: \frac{2\sqrt{x+3} + x}{2\sqrt{x+3}} > 0$

N) $2\sqrt{x+3} + x \geq 0$

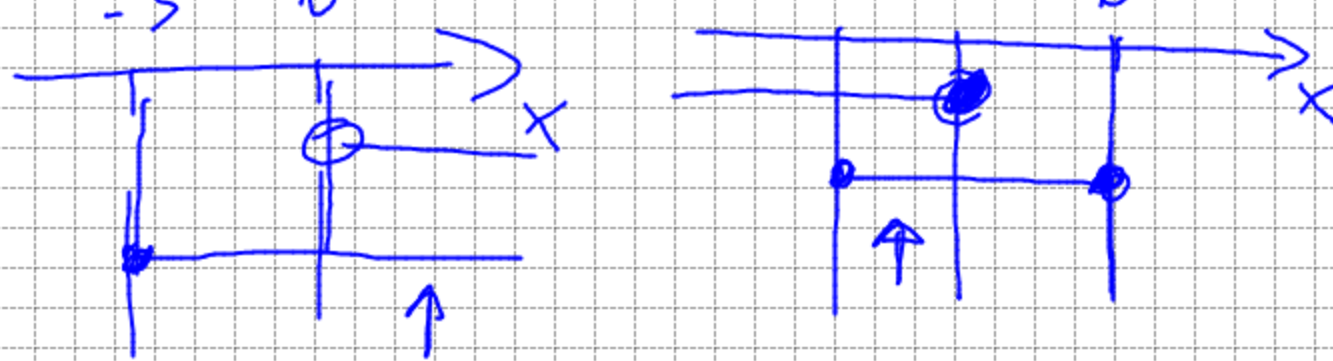
$\sqrt{x+3} \geq -\frac{x}{2}$ $\sqrt{f(x)} \geq g(x)$

$\begin{cases} -\frac{x}{2} < 0 \\ \sqrt{x+3} \geq 0 \end{cases} \cup \begin{cases} -\frac{x}{2} \geq 0 \\ x+3 \geq \left(-\frac{x}{2}\right)^2 \end{cases}$

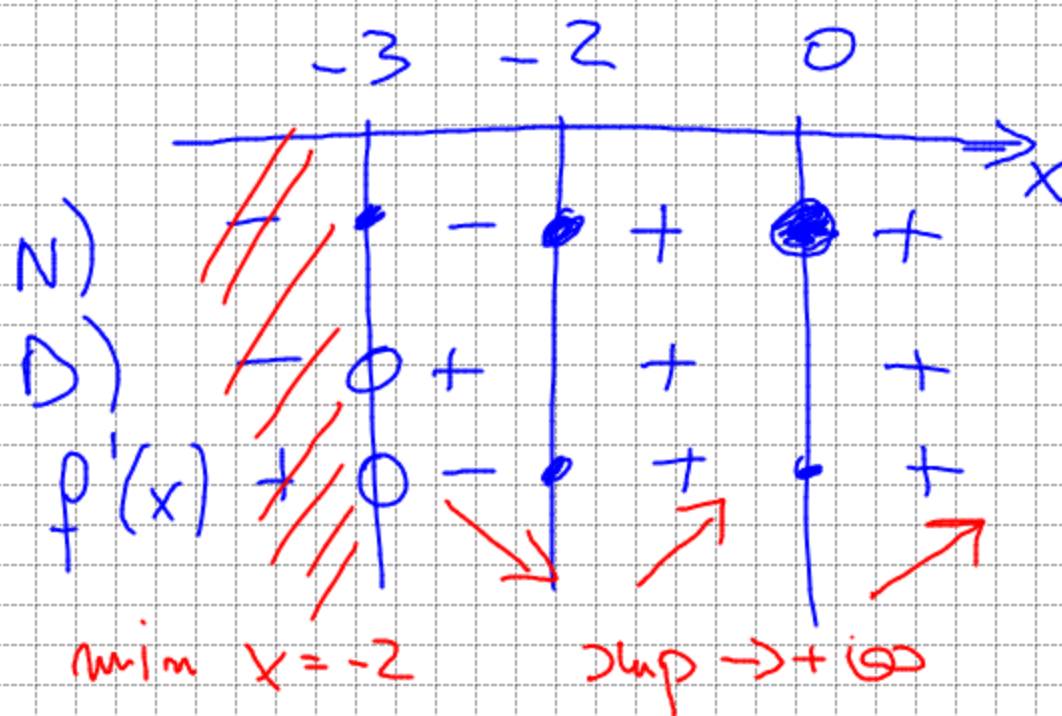


$\begin{cases} x > 0 \\ x \geq -3 \end{cases} \cup \begin{cases} x \leq 0 \\ x+3 \geq \frac{x^2}{4} \end{cases}$

$\begin{cases} x > 0 \\ x \geq -3 \end{cases} \cup \begin{cases} x \leq 0 \\ -x^2 + 4x + 12 \geq 0 \end{cases}$ $x_{1,2} = \frac{-2 \pm \sqrt{4+12}}{-1} = \frac{-2 \pm 4}{-1}$



D) $2\sqrt{x+3} > 0$



min $x = -2$ sup $\rightarrow +\infty$

ESERCIZIO

3/3

$$f(x) = \frac{4x^2 + 1}{x^2 - 2x + 1}$$

$$D_f = \left\{ x \in \mathbb{R} \mid x^2 - 2x + 1 \neq 0 \right\} = (-\infty, 1) \cup (1, +\infty)$$

$$f'(x) = \frac{8x(x^2 - 2x + 1) - (2x - 2)(4x^2 + 1)}{(x^2 - 2x + 1)^2}$$

$$= \frac{\cancel{8x^3} - 16x^2 + 8x - \cancel{8x^3} - 2x + 8x^2 + 2}{(x-1)^4} = \frac{-8x^2 + 6x + 2}{(x-1)^4} \geq 0$$

$$N) -2(4x^2 - 3x - 1) \geq 0$$

$$x_{1,2} = \frac{3 \pm \sqrt{9 + 16}}{8} = \frac{3 \pm 5}{8} = \begin{cases} 1 \\ -\frac{1}{4} \end{cases}$$

$$D) (x-1)^4 > 0$$

