

$$f(x) = \sqrt{x^2 - 4x} - x$$

$$D_f = \{x \in \mathbb{R} / x^2 - 4x \geq 0\} = \{x \in \mathbb{R} / x \leq 0 \cup x \geq 4\}$$

$$(f \circ f)(x) = f(\sqrt{x^2 - 4x} - x)$$

$$D_{(f \circ f)(x)} = \left\{ x \in \mathbb{R} / \sqrt{x^2 - 4x} - x \leq 0 \cup \sqrt{x^2 - 4x} - x \geq 4 \right\}$$

$$\sqrt{x^2 - 4x} \leq x \cup \sqrt{x^2 - 4x} \geq 4 + x$$

⇓

$$\begin{cases} x^2 - 4x \geq 0 \\ x \geq 0 \\ x^2 - 4x \leq x^2 \end{cases}$$

∪

⇓

$$\begin{cases} x^2 - 4x \geq 0 \\ 4 + x < 0 \end{cases}$$

∪

$$\begin{cases} x^2 - 4x \geq (4+x)^2 \\ 4+x \geq 0 \end{cases}$$

$$\begin{cases} x \leq 0 \cup x \geq 4 \\ x \geq 0 \\ x \geq 0 \end{cases}$$

∪

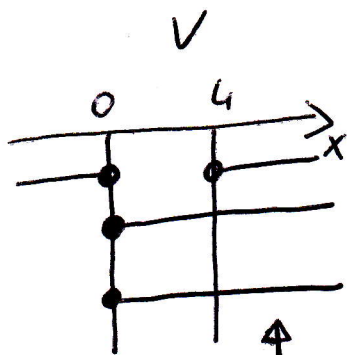
$$\begin{cases} x \leq 0 \cup x \geq 4 \\ x > 4 \end{cases}$$

∪

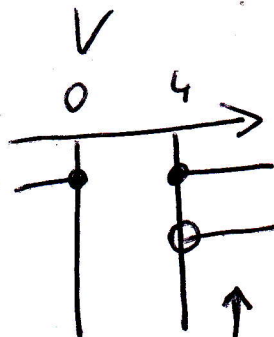
$$\begin{cases} x^2 - 4x \geq 16 + x^2 + 8x \\ x \geq -4 \end{cases}$$

$$12x \leq -\frac{16}{3}$$

$$x \geq -4 \quad x \leq -\frac{4}{3}$$

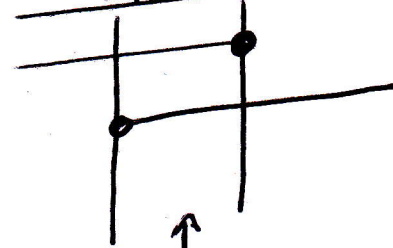


$$x \geq 4 \cup$$



$$x > 4 \cup$$

$$-4 \leq x \leq -\frac{4}{3}$$



$$D_{(f \circ f)(x)} = \boxed{-4 \leq x \leq -\frac{4}{3} \cup x \geq 4}$$