

$$\lim_{x \rightarrow \infty} \left( \frac{x-1}{x+3} \right)^{x+2} = e^{-4}$$

$$\frac{x-1}{x+3} = \frac{(x+3) \cdot 1 - 4}{x+3}$$

$$\begin{array}{r|l} x-1 & x+3 \\ -x-3 & 1 \\ \hline 11-4 & \end{array}$$

$$\lim_{x \rightarrow \infty} \left( 1 - \frac{4}{x+3} \right)^x \left( 1 - \frac{4}{x+3} \right)^2 = (e)^{-4}$$

$$\lim_{x \rightarrow \infty} \left( 1 + \frac{1}{x} \right)^x = e$$

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$$\lim_{x \rightarrow \infty} \left( 1 + \frac{1}{\frac{-x-3}{4}} \right)^{-x} \left( 1 - \frac{1}{x+3} \right)^2 = 1$$

$$\lim_{x \rightarrow \infty} \frac{1}{\left( 1 + \frac{1}{\frac{-x-3}{4}} \right)^{-x-3+3}} \left( 1 - \frac{1}{x+3} \right)^2 =$$

$$\lim_{x \rightarrow \infty} \frac{1}{\left( 1 + \frac{1}{\frac{-x-3}{4}} \right)^{-x-3}} \left( 1 + \frac{1}{-x-3} \right)^2$$

$$-x-3 = z \quad x \rightarrow \infty \quad x = -3-z \quad -3-z \rightarrow \infty$$

$$\lim_{z \rightarrow \infty} \frac{1}{\left[ \left( 1 + \frac{1}{z} \right)^z \right]^4} \left( 1 + \frac{1}{z} \right)^{-1} = \frac{1}{e^4}$$